

$$-\frac{11}{5} - \frac{10}{5} \quad -\frac{2}{5} + \frac{5}{5}$$

[1]

$$(1) \begin{pmatrix} 4 & 3 \\ 5 & 5 \end{pmatrix} \begin{pmatrix} 1 \\ -2 \end{pmatrix} + \begin{pmatrix} 1 \\ -2 \end{pmatrix} = \begin{pmatrix} \frac{4}{5} - \frac{6}{5} \\ -\frac{3}{5} - \frac{4}{5} \end{pmatrix} + \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$= \begin{pmatrix} \frac{3}{5} \\ -\frac{21}{5} \end{pmatrix}$$

$$(2) \begin{pmatrix} 4 & 3 \\ 5 & 5 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} 1 \\ -2 \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$\left. \begin{aligned} \frac{4}{5}x_1 + \frac{3}{5}x_2 + 1 &= 2 \\ -\frac{3}{5}x_1 + \frac{4}{5}x_2 - 2 &= 3 \end{aligned} \right\} \begin{aligned} \times 5 &\rightarrow 4x_1 + 3x_2 + 5 = 20 \dots \textcircled{1} \times 3 \\ &+ \\ -3x_1 + 4x_2 - 10 &= 15 \dots \textcircled{2} \times 4 \end{aligned} \rightarrow$$

$$\begin{aligned} 25x_2 - 25 &= 90 \\ 25x_2 &= 115 \\ x_2 &= \frac{23}{5} \end{aligned}$$

$$\begin{aligned} \frac{4}{5}x_1 + \frac{69}{25} + 1 &= 2 \\ x_1 &= -\frac{4}{5} \end{aligned}$$

$$\vec{X} = \begin{pmatrix} -\frac{4}{5} \\ \frac{23}{5} \end{pmatrix}$$

$$(3) \begin{pmatrix} a \\ b \end{pmatrix} = \begin{pmatrix} 4 & 3 \\ 5 & 5 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} + \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$\begin{aligned} &= \frac{4}{5}a + \frac{3}{5}b + 1 = a \\ &-\frac{3}{5}a + \frac{4}{5}b - 2 = b \end{aligned}$$