

問題 5.1. (1) $\sqrt{5} = 5^{\frac{1}{2}}$ (2) $\frac{1}{81} = 3^{-4}$ (3) $1 = 7^0$ (4) $0.0001 = 10^{-4}$

問題 5.2. (1) $\frac{2}{27}$ (2) 16 (3) $3\sqrt{2}$ (4) 1 (5) $a^2 - b^2$

問題 5.3.

(1) $(\sqrt{8})2\sqrt{2} < 3 (= \sqrt{9})$

(2) $\sqrt[3]{5} < 2 (= \sqrt[3]{8})$

(3) $2^{-3} < 2^{-1} < 2^2$

(4) $\left(\frac{1}{3}\right)^2 < \left(\frac{1}{3}\right)^{-1} < \left(\frac{1}{3}\right)^{-3}$

(5) $9^{-3} < \left(\frac{1}{3}\right)^4 < \left(\frac{1}{3}\right)^0 < 3^2 < \left(\frac{1}{3}\right)^{-3}$

問題 5.4.

$$\begin{aligned}4^{2x-1} = 2^{3x-5} &\iff 2^{2(2x-1)} = 2^{3x-5} \\ &\iff 2^{2(2x-1)-(3x-5)} = 2^0 \\ &\iff 2^{x+3} = 1 \\ &\iff x+3 = 0\end{aligned}$$

よって, 解は $x = -3$.