

問題 7.1.

$$\begin{aligned} \text{sign} \begin{pmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \end{pmatrix} &= +1, & \text{sign} \begin{pmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \end{pmatrix} &= +1, & \text{sign} \begin{pmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \end{pmatrix} &= +1, \\ \text{sign} \begin{pmatrix} 1 & 2 & 3 \\ 1 & 3 & 2 \end{pmatrix} &= -1, & \text{sign} \begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{pmatrix} &= -1, & \text{sign} \begin{pmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \end{pmatrix} &= -1. \end{aligned}$$

問題 7.2. この公式を（3 次正方行列に関する）サラスの公式という；

$$\begin{aligned} \det \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} \\ = a_{11}a_{22}a_{33} + a_{12}a_{23}a_{31} + a_{13}a_{21}a_{32} - (a_{13}a_{22}a_{31} + a_{23}a_{32}a_{11} + a_{33}a_{12}a_{21}) \end{aligned}$$

問題 7.3.

- (1) $\det(A) = 1$
- (2) $\det(B) = 1$
- (3) $\det(C) = 6$

問題 7.4.

- (1) $\det(AB) = 1$
- (2) $\det(C^{-1}) = \frac{1}{6}$

問題 7.5. $\det(P[i, \lambda]) = \lambda$, $\det(Q[i, j]) = -1$, $\det(R[i, j, \lambda]) = 1$